

*“Price Dispersion, Private Uncertainty and
Endogenous Nominal Rigidities”*

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Sticky, Informative Prices

Motivation:

- *Imperfect information provides a rationale for sticky prices: the less firms know, the less they can adjust prices*
- *But, equilibrium prices also reveal the “dispersed bits of incomplete knowledge that we all possess” (Hayek, 1945)*

Question: *How can we maintain imperfect information?
Does stickiness vanish with price dispersion?*

This paper: *Proposes a novel model of nominal frictions
Shows how learning from prices creates stickiness without dispersion*

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Big Picture: A Limit to Informativeness

Market Information:

- *Most economic signals* are the result of market outcomes
- *GDP Statistics, household income, firm prices, asset prices...*
- *All combine and reveal dispersed information*

But *what limits the informativeness of market information?*

⇒ that market outcomes are the result of complicated GE

Gaetano shows how *GE feedbacks can help limit the informativeness of market outcomes*

⇒ *creates disagreement and misallocation*

⇒ *helps makes market outcomes persistent*

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A Simple Example

Basic Setup:

- Simplified two-period *CARA-Normal asset price model*
- *Risky asset* with terminal payoff $\theta \sim N(0, 1)$ in supply $S = \alpha\theta$ and a *riskless asset* with normalized zero return
- *Stark* information structure: $p_i = p + \eta_i$, $\eta_i \sim N(0, 1/\tau_\eta)$

Equilibrium Conditions:

1. *Demand for Asset:* $D_i = (\mathbb{E}_i[\theta] - p) \nabla_i [\theta - p]^{-1}$
2. *Market Equilibrium:* $\int_0^1 D_i(p; p_i) di = S(\theta)$

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Equilibrium Characterization

Equilibrium Asset Price:

$$p_i = \bar{\mathbb{E}}[\theta] - \delta\theta + \eta_i \stackrel{!}{=} k_0\theta + \eta_i$$

- *Supply Offset:* $\delta = \alpha \bar{\mathbb{V}}[\theta - p]$
- *Informativeness:* $s_{ip} = \theta + (1/k_0)\eta_i$

Equilibrium Solution:

$$p_i = \frac{\tau_\eta k_0^2 - \alpha}{1 + \tau_\eta k_0^2} \theta + \eta_i \stackrel{!}{=} k_0\theta + \eta_i$$

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Dispersed Limit Equilibria

Fixed-Point Condition:

$$k_0 = \frac{\tau_\eta k_0^2 - \alpha}{1 + \tau_\eta k_0^2}$$

- *Third-order polynomial in k_0*
- *Descartes' Rule of Signs: one or three equilibria*

Multiple Equilibria: *Strategic complementarity*

Dispersed Limit Equilibria:

$$p = \bar{\mathbb{E}}[\theta] - \delta\theta = k_0\theta$$

- $\lim_{\tau_\eta \rightarrow \infty} k_0^1 = 1 \sim$ *full information*
- $\lim_{\tau_\eta \rightarrow \infty} k_0^{2,3} = 0 \sim$ *zero information!*

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Endogenous Nominal Stickiness

Equilibrium Selection:

$$\hat{\mathbb{E}}_i^n[\theta] \xrightarrow{n} \mathbb{E}^{DLE}[\theta] = 0$$

- *DLE locally learnable*
- *... and unique rationalizable outcome*

Economic Consequences:

- *Equilibrium price is sticky*
- *... and does not transmit information*
- *Equilibrium allocations \neq first best*

Endogenous Equilibrium Stickiness!

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A Bird's Eye View

Model Setup:

- Monopolistic competitive *Lucas island model*
- Continuum of firms preset labor and capital
- Uncertain about money supply θ and preference shock ξ_i

Learning from Prices:

Allocative vs informational trade-off through R

\implies *little price dispersion makes monetary policy potent*

Comments:

1. *Allocative vs Informational Role*
2. *Symmetric Information: Another Candidate?*
3. *Natura Non Facit Saltus*

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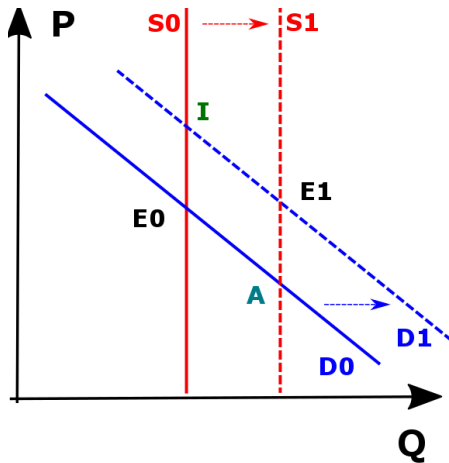
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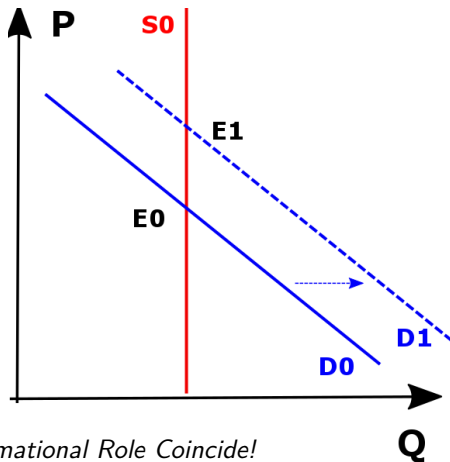
Fundamental Value Shock:



Small Noise Maintains Imperfect Information!

Allocative vs Informational Role

A Pure Demand Shock ($\alpha = 0$):



Allocative and Informational Role Coincide!

Nature of Disturbance? Supply vs Demand Competition?

Unexplored Consequences

Dispersed Information Equilibria:

- *Sticky local prices* $r_i \rightarrow 0$
- *Powerful monetary policy*

Cross-sectional Dispersion: ...increases both for productivity and for consumer prices in recessions (Bloom '09; Vavra, '14)

Empirical Consequences:

$$\frac{\partial^2 y}{\partial m \partial \sigma_\theta} < 0 \quad \text{vs} \quad \frac{\partial^2 y^{li}}{\partial m^{li} \partial \sigma_\theta^{li}} > 0$$

- *Theoretically:* < 0 (Vavra, '14)
- *Empirically:* < 0 (Tenreyro and Thwaites, '17)

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Natura Non Facit Saltus

Multiple Limit Equilibria:

- *Full information*
- *Dispersed information*

Correct Limit Equilibrium?

Leibniz' Axiom:

- *Learning limit vs mathematical limit?*
- *Payoff dominance (Harsanyi and Selten, '88)?*

A Failure of Coordination?

Final Remarks

Conclusion:

- Since **Lucas (1972)** and **Grossman and Stiglitz (1980)** focus on how people infer **information** from **market prices**
- Yet, the mere presence of **market interactions** has profound implications for how prices **respond** to unobserved **fundamentals**
- **Gaetano** turns our attention to the **important role played** by such **market interactions** in *limiting price informativeness*
- **clear upside potential**

Rubinstein (1989): *Almost Perfect Information \neq Perfect Information*

Thank you for your time and attention!