# **Lecture 4: Labour economics**

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### The monopsony model

- Barriers to free entry of firms
- Limited mobility of labour
- A monopsonist can hold down wages below the competitive wage

### **Examples**

- Single-firm towns ("bruksorter")
- The labour-market for nurses
  - just one hospital in a region
  - cartel of regions ("landsting") earlier in Sweden

# The basic monopsony model

- Labour supply  $L^s(w) = G(w)$
- An employed person produces y

# **Decision problem of a monopsonist**

Max 
$$\pi(w) = L^{s}(w)(y - w)$$
  
 $L_{1}^{s}(y - w) - L^{s} = 0$ 

$$\frac{L_1^s}{L^s} w(\frac{y}{w} - 1) - 1 = 0$$

Define 
$$\frac{\partial L^s}{\partial w} \cdot \frac{w}{L_s} = \eta_w^L$$
 = the elasticity of labour supply

Hence:

$$\eta_w^L \left[ \frac{y}{w} - 1 \right] - 1 = 0$$

$$w = \frac{\eta_w^L}{\eta_w^L + 1} y$$

$$\frac{\eta_w^L}{\eta_w^L + 1}$$
 < 1 implies that  $w < y$ , i.e. that the monopsonist

sets a lower wage than the competitive wage

The monopsonistic wage coincides with the competitive wage only if  $\,\eta_{_w}^{^L} \to \infty$  in which case

$$w = \frac{\eta_w^L}{\eta_w^L + 1} = \frac{1}{1 + \frac{1}{\eta_w^L}} \quad y \to y$$

- Otherwise the monopsonist gains by lowering the wage below the competitive wage
- This reduces the labour supply and hence output and employment. But the loss from this is outweighed by the savings on the wage bill.

#### **Isoprofit curve**

$$\pi = L(y - w) = \overline{\pi}$$

$$dL(y - w) - Ldw = 0$$

$$\frac{dL}{dw} = \frac{L}{y - w} \qquad \frac{dL}{dw} > 0 \text{ for } y > w$$

Profit maximisation at the tangency point between an isoprofit curve and the labour supply schedule

- A minimum wage if it is not too high raises both the wage and employment in a monopsonistic market
- Non-monotonic relationship between minimum wage and employment in a monopsonistic market

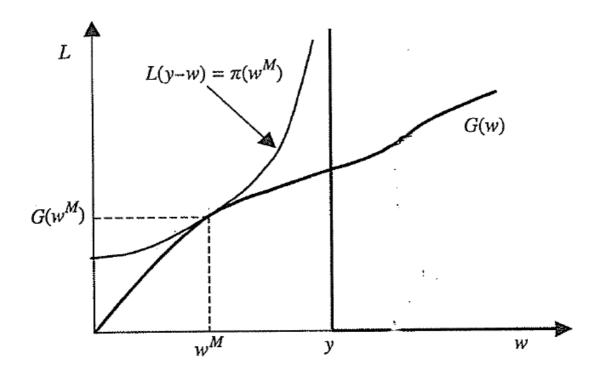


FIGURE 5.4
The monopsony model.

#### Sources of monopsony power

- Workers must have limited mobility
  - transportation cost
  - qualifications that cannot be used elsewhere
- Entry costs must prevent entry of competitors

# Simple game-theoretic model for why the existence of entry costs can uphold a monopsony

N firms can enter
c is the entry cost
Each worker produces y

Stage 1: entry decision Stage 2: wage decision

- Solve the model backwards
- If only one firm it sets the monopsony wage
  If there are n > 1 competitors, firm i sets its wage  $w_i$  so as to maximise its profit

 $\pi_i = L_i (y-w_i)$  taking the wages of other firms as given

Employment  $L_i$  in firm i depends on all wages  $(w_i, \ldots, w_n)$  in the following way:

$$L_i = L^s(w_i) \text{ if } w_i > w_j, \quad \forall j \neq i$$

 $L_i = (1/J)L^s(w_i)$  if *i* sets the highest wage together with *J*-1 other firms, 1 < J < n

 $L_i = 0$  if there exists one firm  $j \neq i$  which sets  $w_i < w_j$ 

- All wages equal to y is a Nash equilibrium
- Then each firm has zero profits and cannot improve its profits
  - with a lower wage all labour disappears
  - with a higher wage it makes a loss
- No single firm can set  $w_i < y$ .
  - it would then make a profit
  - hence it would pay for a competitor to raise the wage above  $w_i$  and capture the whole labour supply
  - This is so-called <u>Bertrand competition</u>, which forces the wage up to the competitive level

### **Stage 1 decision**

- Each firm knows that
  - (i) it will make zero profits with competitors present in the market
  - (ii) it will make monopsony profits if it alone enters
- Once a firm has entered it does not pay for any other firm to enter
  - profits will be zero
  - but an entry cost c has to be paid
  - the first firm (if possibilities to enter come sequentially) chooses to enter if  $\pi(w^M) > c$ .
- Extreme assumptions here regarding Bertrand competition but good illustration of how entry costs may give rise to monopsony and wage differences to other sectors unrelated to productivity.

### **Collective bargaining**

- Common assumption for unions: identical members
- N identical members in the union's "labour pool"
- Indirect utility function for the individual, increasing in income
- Every member supplies one unit of labour if the real wage w exceeds the reservation wage  $\overline{w}$  (= income of an unemployed person)
- L = Labour demand
- Same probability of getting a job for every union member = L/N if L < N and unity if  $L \ge N$
- Probability of unemployment  $(1 \frac{L}{N})$  if L < N and zero if  $L \ge N$ .

#### Union objective

Maximise the expected utility of members

$$\nu_{s} = l\nu(w) + (1-l)\nu(\overline{w}) \qquad l = \operatorname{Min}(1, L/N)$$

If N is exogenous, this is equivalent to maximising the unweighted sum of members' utilities:

$$L\nu(w) + (N-L)\nu(\overline{w})$$

If workers are risk-neutral so that  $\nu(w) = w$  and  $\nu(\overline{w}) = \overline{w}$ , unions maximise the rent from unionisation:

$$lw + (1-l)(\overline{w}) = l(w-\overline{w}) + \overline{w}$$

If  $\overline{w} = 0$ , this is equivalent to maximising the wage bill: lw

Table 3.1

Coverage of collective agreements and unionisation<sup>a)</sup>

	Total economy (2001)		Market sector (mid 1990s)		
Country	Coverage	Unioni- sation	Coverage	Unioni- sation	
Old EU member states					
Austria	98	40	97	34	
Belgium	100	69	82	44	
Denmark	85	88	52	68	
Finland	90	79	67	65	
France	90	9	75	< 4	
Germany	67	30	80	25	
Greece		32	• • • • • • • • • • • • • • • • • • • •		
Ireland				43	
Italy		35		36	
Luxemburg	60	50			
Netherlands	78	27	79	19	
Portugal	62	30	80	< 20	
Spain	81	15	67	< 15	
Sweden	94	79	72	77	
UK <sup>b)</sup>	36	29	35	19	
New EU member states					
Cyprus	65-70	70			
Czech Republic	25-30	30			
Estonia	29	15			
Hungary	34	20			
Latvia	< 20	30			
Lithuania	10-15	15			
Malta	60-70	65			
Poland	40	15			
Slovakia	48	40			
Slovenia	100	41			
Other countries					
Australia	22 (23)c)	23			
Canada	32	30g)			
Japan	. 21	22h)	21	24	
New Zealand	45 <sup>d)</sup>	22			
Norway	70-77°)	55h)	62	44	
Switzerland	53°	23h)	50	22	
US	15	14 <sup>h)</sup>	13	10	

Notes: a Coverage refers to the percentage of employees covered by collective agreements and unionisation to the percentage of employees with union membership; b Figures do not include Northern Ireland; The parenthesis refers to the coverage of wage awards (see Section 1.1) and to 2000; d 1997; 2000–01; 1994; 2000; 1996–98.

**EEAG Report 2004** 

Chapter 3

**Fig. 3.1** UNIONISATION TRENDS IN WESTERN EUROPE AND THE UNITED STATES Union density 50.0 45.0 Western Europe 40.0 35.0 30.0 25.0 **United States** 20.0 15.0 60 62 64 66 68 70 72 74 76 78 80 82 84 86 88 90 92 94 96 98 Note: Union density (union membership relative to employment) for Western Europe is a weighted average of Austria, Belgium, Denmark, Finland, France, western Germany, Ireland, Italy, the Netherlands, Norway. Sweden, Switzerland and the United Kingdom. Source: Ebbinghaus and Visser (2000). Chapter 3 **EEAG Report 2004** 

Table 3.2  Bargaining levels							
Country	National guidelines	Inter- sectoral level	Sectoral level	Enterprise level			
Old EU member states							
Austria	Pattern bargaining		XXX	X			
Belgium	Centrally agreed guidelines for wage increases with the government 2003-04	XXX	X	x			
Denmark	Pattern bargaining	XX	XX	X			
Finland	Tripartite national pay agreement 2003-04	XXX	XX	X			
France			×	xx			
Germany	Pattern bargaining		XXX	X			
Greece	National general collective agreement 2002-03	XX	XXX	X			
Ireland	Tripartite national pay agreement 2003-04	XXX	X	x			
Italy	Social pacts with government 1993 and 1998 setting	222	xx	x			
Italy	guidelines for the wage-bargaining process		AA	Λ			
Luxemburg	guidenines for the wage-bargaining process		XX	XX			
Netherlands	Controlly corond colling for word in second with	XX	xxx	X			
Netherlands	Centrally agreed ceiling for wage increases with government 2003; tripartite national wage freeze 2004-05	***	****	Λ.			
Portugal	1		XXX	x			
Spain	Centrally agreed guidelines for wage increases 2003	XX	XXX	X			
Sweden	Intersectoral agreements setting guidelines for the wage-bargaining process; pattern bargaining	AA	XXX	хх			
UK			X	XXX			
New EU member states							
Cyprus			XXX	X			
Czech Republic	Tripartite national agreements on minimum wages		X	XXX			
Estonia	Tripartite national agreements on minimum wages		x	XXX			
Hungary	National guidelines for wage increases agreed with	x	xx	XXX			
	government and tripartite national agreements on						
E-rest.	minimum wages	**	27	10/1/			
Latvia	Tripartite national agreements on minimum wages	X	X	XXX			
Lithuania			X	XXX			
Malta				XXX			
Poland	National guidelines for wage increases agreed with government and tripartite national agreements on		Х	XXX			
Slovakia	minimum wages		~~	~			
Slovakia	Tripartite national agreements on minimum wages	******	XX	X			
Siovenia	Tripartite national pay bargains	XXX	XX	X			
Other countries	L						
Australia	National wage awards for minimum wages	X	XX	XXX			
Japan	Pattern bargaining			XXX			
New Zealand	1		X	XXX			
Norway	Pattern bargaining; tripartite agreement on guidelines for wage increases 2003	XX	XXX	X			
Switzerland			X	XX			
US				·xxx			

**EEAG Report** 

X = existing level

Sources: Industrial Relations in the EU Member States and Candidate Countries (2002), Collective Bargaining Coverage and Extension Procedures (2002), individual Eiroline country reports. For New Zealand: Bray and Walsh (1998).

Chapter 3

- Assumption of identical union members is convenient and has microeconomic underpinnings
- But in reality members are heterogeneous
- Restrictive assumptions necessary for collective decisionmaking
  - majority decisions
  - sincere voting: no attempts to influence voting by announcing intentions beforehand
  - voting on a single question
  - single-peaked preferences
  - then the median-voter theorem can be applied
- Restrictive assumption for union decision-making
  - voting only about the wage
- Conflicts between union leadership and membership
  - leadership may want to maximise union size
  - union size may increase with employment
  - boss-dominated unions show more wage restraint

# **Empirical studies of union goals**

# Stone-Geary utility function

$$\nu_{s} = (w - w_{0})^{\theta} (L - L_{0})^{1-\theta}$$
  $\theta \in [0,1]$ 

#### **Special cases**

$$\theta = \frac{1}{2}$$
,  $w_0 = 0$ ,  $L_0 = 0 \Rightarrow$  wage bill maximisation

$$\theta = \frac{1}{2}$$
,  $w_0 = \overline{W}$ ,  $L_0 = 0 \Rightarrow$  rent maximisation

#### Pencavel (1984) used Stone-Geary utility function

### **Decision problem**

$$\max_{w} \ \nu_{s} = (w - w_{0})^{\theta} (L - L_{0})^{1-\theta}$$

s.t. 
$$L = \alpha_0 + \alpha_1 (w/r_1) + \alpha_2 (r_2/r_1) + \alpha_3 x + \alpha_4 D$$

 $r_1$  = output price

 $r_2$  = production cost

x = output

D = Dummy variable

# **FOC**:

$$\frac{\theta}{\theta-1} = \frac{\alpha_{_{1}}(w-w_{_{0}})}{r_{_{1}}(L-L_{_{0}})}$$

# Estimation of labour demand function and FOC gives estimates of $\theta$ , $w_0$ , $L_0$ , $\alpha_0$ , $\alpha_1$ , $\alpha_2$ , $\alpha_3$ and $\alpha_4$ .

- Not rent or wage bill maximisation
- Different  $\theta$ , but tendency for  $\theta$  to be low
- $w_0$  and  $L_0$  increase with the size of the union

### **Carruth and Oswald (1985)**

- Rejection of risk neutrality (and wage bill and rent maximisation)
- CRRA =  $-w\nu$  " $(w)/\nu$  ' $(w) \approx 0.8$
- Risk neutrality implies  $-w\nu''(w)/\nu'(w) = -w\cdot 0/1 = 0$
- $\frac{w^{1-\delta}}{1-\delta}$ ;  $\delta$  is CRRA

# Standard right-to-manage model

- Bargaining about wages
- Employer determines employment unilaterally

## **Union objective**

$$\nu_s = l\nu(w) + (1-l)\nu(\overline{w})$$
  $1 = \text{Min}(1, L/N)$ 

# Firm profit

$$\pi = R(L) - wL$$
  $R' > 0, R'' < 0$ 

# Labour demand from profit maximisation

$$\frac{\partial \pi}{\partial L} = R'(L) - w = 0$$

$$w = R'(L)$$

$$L^{d}(w) = R'^{(-1)}(w)$$

# In case of disagreement

- Workers get the utility of unemployed persons
- Firms get zero profit

 $\gamma$  denotes relative bargaining strength of the union:  $0 \le \gamma \le 1$ 

# Apply Nash bargaining solution

Max 
$$(\nu_{s} - \nu_{0})^{\gamma} (\pi - \pi_{0})^{1-\gamma}$$

 $\pi_{_{0}}$ = Profit in case of disagreement

 $\nu_{_0}$  = union utility in case of disagreement

$$\begin{split} \pi_{_0} &= 0 \\ \nu_{_0} &= \ell \nu(\overline{w}) + (1 - \ell) \nu(\overline{w}) = \nu(\overline{w}) \\ \nu_{_s} - \nu_{_0} &= \ell \nu(w) + (1 - \ell) \nu(\overline{w}) - \nu(\overline{w}) = \ell(\nu(w) - \nu(\overline{w})) = \\ &= \frac{L^d}{N} \big[ \nu(w) - \nu(\overline{w}) \big] \end{split}$$

$$\operatorname{Max}_{w} \quad \left[ L^{D}(w) \right]^{\gamma} \left[ \nu(w) - \nu(\overline{w}) \right]^{\gamma} \left[ \pi(w) \right]^{1-\gamma} \\
\text{with} \quad \pi(w) = R \left[ L^{D}(w) \right] - wL^{d}(w) \\
\text{s.t.} \quad L^{d}(w) \leq N \quad \text{and} \quad w \geq \overline{w}$$

Solve by taking logs and then differentiate w.r.t. w

**FOC**:

$$\frac{\gamma}{L^{d}(w)} \frac{dL^{d}(w)}{dw} + \frac{\gamma \nu'(w)}{\nu(w) - \nu(\overline{w})} + \frac{(1-\gamma)}{\pi(w)} \frac{d\pi(w)}{dw} = 0$$

Note: Mistake in formula on page 394:

Second term should be

$$\frac{\gamma \nu'(w)}{\nu(w) - \nu(\overline{w})}$$
not
$$\frac{\gamma w \nu'(w)}{\nu(w) - \nu(\overline{w})}$$

Let 
$$\eta_w^L = -(w/L)(dL/dw)$$
  
 $\eta_w^\pi = -(w/\pi)(d\pi/dw)$ 

# Absolute values of wage elasticities of labour demand and profits

Posit 
$$\eta_{w}^{L} = \eta_{w}^{L}(w, z_{L})$$
  $\partial \eta_{w}^{L} / \partial_{L}^{z} > 0$ 

$$\eta_{w}^{\pi} = \eta_{w}^{\pi}(w, z_{\pi}) \qquad \partial \eta_{w}^{\pi} / \partial_{\pi}^{z} > 0$$

$$\phi(w, \overline{w}, z_{L}, z_{\pi}, \gamma) = -\gamma \eta_{w}^{L} - (1 - \gamma) \eta_{w}^{\pi} + \frac{\gamma w \nu'(w)}{\nu(w) - \nu(\overline{w})} = 0$$

$$(1) \qquad (2) \qquad (3)$$

- (1) Employment loss from wage increase
- (2) Profit loss from wage increase
- (3) Income gain for employed workers from wage increase

# Monopoly union assumption

$$\gamma = 1 \Rightarrow \eta_{w}^{L} + \frac{w\nu'(w)}{\nu(w) - \nu(\overline{w})} = 0$$

- Still interior solution
- Trade union balances income gain for employed workers against employment loss from wage increase

# SOC for a maximum is $\,\phi_{_{\scriptscriptstyle W}} < \,0\,$

$$x = (\overline{w}, z_{L}, z_{\pi}, \gamma)$$

$$\phi_{w} dw + \phi_{x} dx = 0$$

$$\frac{dw}{dx} = -\frac{\phi_{x}}{\phi_{w}}$$

$$\phi_{w} < 0 \Rightarrow \operatorname{sgn} \frac{dw}{dx} = \operatorname{sgn} \phi_{x}$$

$$\phi_{\gamma} = -\eta_{w}^{L} + \eta_{w}^{\pi} + \frac{w\nu'(w)}{\nu(w) - \nu(\overline{w})}$$

#### From FOC we can derive:

$$-\eta_{w}^{L} + \frac{w\nu'(w)}{\nu(w) - \nu(\overline{w})} = \frac{1 - \gamma}{\gamma} \eta_{w}^{\pi}$$

# Substitution into expression for $\phi_{_{\gamma}}$ gives

$$\phi_{\gamma} = \eta_{w}^{\pi} + \frac{1-\gamma}{\gamma} \eta_{w}^{\pi} = \frac{\eta_{w}^{\pi}}{\gamma} > 0$$

$$\because \frac{dw}{d\gamma} > 0$$

• Larger union bargaining power raises the wage

$$\phi_{\overline{w}} = \frac{\gamma w \nu'(w)}{\left[\nu(w) - \nu(\overline{w})\right]^2} \cdot \frac{\partial \nu}{\partial \overline{w}} > 0$$

• An income increase for a jobless person raises the wage

$$\phi_{\eta_w^L} = -\gamma < 0$$

• An increase in the labour demand elasticity lowers the wage

$$\phi_{\eta_w^{\pi}} = -(1-\gamma) < 0$$

• An increase in the profit elasticity lowers the wage

# **Rewrite FOC:**

$$\frac{\nu(w) - \nu(\overline{w})}{w\nu'(w)} = \frac{\gamma}{\gamma \eta_w^L + (1 - \gamma) \eta_w^{\pi}} \equiv \mu_s$$

# No bargaining power for union: $\gamma = 0$

Hence: 
$$\nu(w) = \overline{\nu}(\overline{w})$$

$$w = \overline{w}$$

• Employed workers only get a wage equal to the income of the unemployed

# No bargaining power for the employer: $\gamma = 1$

$$\frac{\nu(w) - \nu(\overline{w})}{w\nu'(w)} = \frac{1}{\eta_w^L}$$

• The mark-up factor only depends on the elasticity of labour demand.

#### Union indifference curves in w, L-space

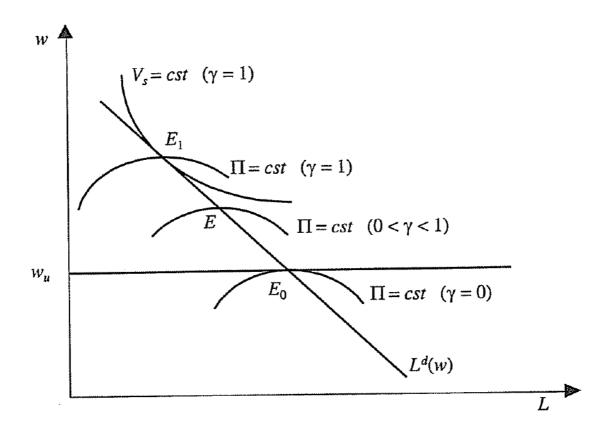
$$\overline{U} = L[\nu(w) - \nu(\overline{w})]$$

$$0 = L\nu'(w)dw + dL[\nu(w) - \nu(\overline{w})]$$

$$\frac{dw}{dL} = \left| \frac{1}{\overline{U} = const} \right| = -\frac{\left[\nu(w) - \nu(\overline{w})\right]}{L\nu'(w)} \le 0$$

$$\frac{d^2w}{dL^2} = \left| \frac{1}{U = const} \right| = \frac{\left[\nu(w) - \nu(\overline{w})\right]}{L^2 \left[\nu'(w)\right]^2} \left\{ 2\nu'(w) - \nu''(w) \frac{\left[\nu(w) - \nu(\overline{w})\right]}{\nu'(w)} \right\} \ge 0$$

Union indifference curves are negatively sloped and convex.



The right-to-manage model.

#### **Isoprofit curves**

$$\overline{\pi} = R(L) - wL$$

$$R'(L)dL - wdL - Ldw = 0$$

$$\frac{dw}{dL} \bigg|_{\pi = \overline{\pi}} = \frac{R'(L) - w}{L}$$

$$d\left[\frac{dw}{dL} \mid_{\pi=\overline{\pi}}\right] = \frac{L[R''(L)dL - dw] - dL[R'(L) - w]}{L^2} =$$

$$\frac{d^2w}{dL^2} \Big|_{\pi=\overline{\pi}} = \frac{LR''(L)}{L^2} - \frac{\frac{dw}{dL}}{L^2} - \frac{\left[R'(L) - w\right]}{L^2}$$

Substitute 
$$\frac{R'(L)-w}{L}$$
 for  $\frac{dw}{dL}$ :

$$\frac{d^{2}w}{dL^{2}} \bigg|_{\pi = \overline{\pi}} = \frac{LR''(L)}{L^{2}} - \frac{R'(L) - w}{L^{2}} - \frac{R'(L) - w}{L_{2}}$$

$$= \frac{LR''(L) - 2[R'(L) - w]}{L^2}$$

- Choosing L to maximise profit implies R'(L) = w. Hence isoprofit curve is horizontal where it intersects the labour demand schedule.
- At intersection with labour demand schedule, R'(L) = w.

Hence 
$$\frac{d^2w}{dL^2}\Big|_{\pi=\overline{\pi}} = \frac{R''(L)}{L} < 0.$$

Isoprofit curves are concave there, which imply maxima.

### **General FOC:**

$$-\gamma \eta_{w}^{L} - (1-\lambda) \eta_{w}^{\pi} + \frac{\gamma w \nu'(w)}{\nu(w) - \nu(\overline{w})} = 0$$
 (A)

- If  $\eta_w^L$ ,  $\eta_w^\pi$ ,  $\gamma$  and  $\overline{w}$  are constants, then the real wage w is constant as well. It will not be affected by an iso-elastic shift of the labour demand schedule (for example because of a productivity shock).
- Constant  $\eta_{_w}^{^L}$  and  $\eta_{_w}^{^\pi}$  will occur if the revenue function is Cobb-Douglas.

# **Simplified model**

$$\pi = R(L) - wL = \frac{AL^{\alpha}}{\alpha} - wL \qquad \alpha \in (0, 1)$$

# **Profit maximisation gives:**

$$\frac{\partial \pi}{\partial L} = AL^{\alpha-1} - w = 0$$

$$L = \left(\frac{w}{A}\right)^{\frac{1}{\alpha-1}}$$

Then:

$$\pi = \frac{A}{\alpha} \cdot \left(\frac{w}{A}\right)^{\frac{\alpha}{\alpha-1}} - w \cdot \left(\frac{w}{A}\right)^{\frac{1}{\alpha-1}}$$

$$\pi = w^{\frac{\alpha}{\alpha-1}} \cdot \frac{1-\alpha}{\alpha} A^{\frac{1}{\alpha-1}}$$

Hence:

$$\eta_{w}^{L} = -\frac{\partial L}{\partial w} \cdot \frac{L}{w} = \frac{1}{1-\alpha}$$

$$\eta_{w}^{\pi} = -\frac{\partial L}{\partial w} \cdot \frac{w}{\pi} = \frac{\alpha}{1-\alpha}$$

Also assume that  $\nu(w) = w$  and  $\nu(\overline{w}) = \overline{w}$ Then  $\nu'(w) = 1$ 

FOC (A) then becomes:

$$-\gamma \cdot \frac{1}{1-\alpha} - (1-\gamma)\frac{\alpha}{1-\alpha} + \frac{\gamma w}{w-\overline{w}} = 0$$

Solving for w gives:

$$w = \frac{\gamma + \alpha(1 - \gamma)}{\alpha} \overline{w}$$

The wage is set as a mark-up on the income of an unemployed, since  $\gamma + \alpha(1-\gamma) > \alpha \Leftrightarrow \gamma(1-\alpha) > 0$ , which must hold.

Especially simple form in monopoly-union case, i.e. if  $\gamma = 1$ 

Then 
$$w = \frac{\overline{w}}{\alpha}$$

We have:

$$\eta_{\rm w}^{\rm L} = \frac{1}{1 - \alpha}$$

Hence:

$$1 - \alpha = \frac{1}{\eta_{w}^{L}}$$

$$\alpha = 1 - \frac{1}{\eta_{w}^{L}} = \frac{\eta_{w}^{L} - 1}{\eta_{w}^{L}}$$

Thus:

$$w = \left[1 - \frac{1}{\eta_{w}^{L}}\right]^{-1} \overline{w}$$

$$w = \frac{\eta_w^L}{\eta_w^L - 1} \overline{w}$$

Analogy to monopoly price setting with price as a mark-up over marginal cost

 $\eta_{_{\scriptscriptstyle W}}^{^{\scriptscriptstyle L}}>1\,$  is always the case with Cobb-Douglas production function,

as 
$$\eta_{w}^{L} = \frac{1}{1-\alpha}$$
 and  $0 < \alpha < 1$ .

# General equilibrium model

$$w_{i} = \frac{\gamma + \alpha(1 - \gamma)}{\alpha} \overline{w}$$

- Assume mobility in the labour market. An unemployed in a given firm (labour pool) can either find a job in another firm (labour pool) or become unemployed.
- Symmetric economy with a large number of firms.
- Look at wage-setting in firm i.
- Probability of getting a job in another firm = l = the economy-wide employment rate = employment/labour force.
- Probability of not finding a job elsewhere = 1-l.
- A worker who finds a job elsewhere receives the wage w.
- If unemployed, the worker receives the unemployment benefit b.

 $\overline{w}$  = the expected income if not employed in firm i = alternative income

$$\overline{w} = \ell w + (1 - \ell)b$$

Hence:

$$w_{i} = \frac{\gamma + \alpha(1-\gamma)}{\alpha} \left[ \ell w + (1-\ell)b \right]$$

In a symmetric equlibrium  $w_i = w$ 

Denote the mark-up factor 
$$\frac{\gamma + \alpha(1-\gamma)}{\alpha} = m$$

Then:

$$w = m \left[ \ell w + (1 - \ell) \right] b$$

$$w = \frac{m(1 - \ell)}{1 - m\ell} b$$
 (B)

• The wage is still a mark-up over the unemployment benefit as  $m(1-\ell) > 1-m\ell \iff m>1$ 

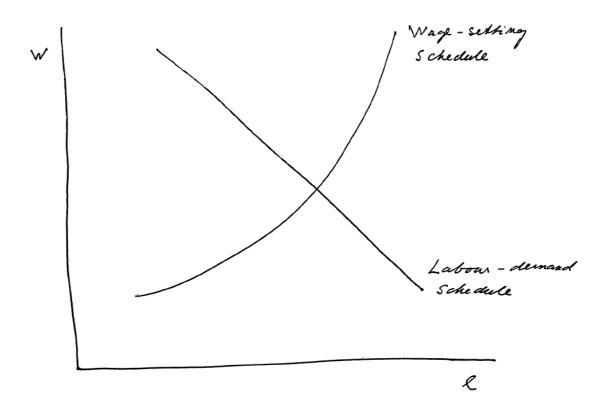
• The overall wage in the economy, w, is positively related to employment as:

$$\frac{\partial w}{\partial \ell} = \frac{m(m-1)}{(1-m\ell)^2} > 0$$

# w = f(l) is called a <u>wage-setting schedule</u>

# It shifts upwards if:

- **(1)** γ↑
- (2)  $\dot{b}\uparrow$
- Equilibrium employment is given by intersection between the wage-setting schedule and the labour-demand schedule.
- Shift of labour-demand schedule affects the equilibrium employment rate.



# **Key question:** How is the unemployment benefit determined?

- 1. Constant in real terms
- 2. Constant replacement rate r, so that b = rw

# **Constant replacement rate:**

$$w = \frac{m(1-\ell)}{1-m\ell}b$$

$$w = \frac{m(1-\ell)}{1-m\ell}rw$$

$$1 = \frac{m(1-\ell)}{1-m\ell}r$$

$$\ell = \frac{1 - rm}{m(1 - r)}$$

$$\frac{\partial \ell}{\partial r} = \frac{m(1-m)}{(m-r)^2} < 0$$

- Vertical wage-setting schedule determined by labour-market institutions only (here r and  $\gamma$ )
- An increase in the replacement rate reduces the employment rate
- Shifts in labour demand have no effect on the equilibrium employment rate.

