# Lecture 4: Labour economics 

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The monopsony model

- Barriers to free entry of firms
- Limited mobility of labour
- A monopsonist can hold down wages below the competitive wage


## Examples

- Single-firm towns ("bruksorter")
- The labour-market for nurses
- just one hospital in a region
- cartel of regions ("landsting") earlier in Sweden


## The basic monopsony model

- Labour supply $L^{s}(w)=G(w)$
- An employed person produces $y$


## Decision problem of a monopsonist

$$
\begin{array}{ll}
\underset{w}{\operatorname{Max}} & \pi(w)=L^{s}(w)(y-w) \\
& L_{1}^{s}(y-w)-L^{s}=0 \\
& \frac{L_{1}^{s}}{L^{s}} w\left(\frac{y}{w}-1\right)-1=0
\end{array}
$$

Define $\frac{\partial L^{s}}{\partial w} \cdot \frac{w}{L_{s}}=\eta_{w}^{L}=$ the elasticity of labour supply
Hence:
$\eta_{w}^{L}\left[\frac{y}{w}-1\right]-1=0$

$$
w=\frac{\eta_{w}^{L}}{\eta_{w}^{L}+1} y
$$

$\frac{\eta_{w}^{L}}{\eta_{w}^{L}+1}<1$ implies that $w<y$, i.e. that the monopsonist
sets a lower wage than the competitive wage

The monopsonistic wage coincides with the competitive wage only if $\eta_{w}^{L} \rightarrow \infty$ in which case

$$
w=\frac{\eta_{w}^{L}}{\eta_{w}^{L}+1}=\frac{1}{1+\frac{1}{\eta_{w}^{L}}} \mathrm{y} \rightarrow \mathrm{y}
$$

- Otherwise the monopsonist gains by lowering the wage below the competitive wage
- This reduces the labour supply and hence output and employment. But the loss from this is outweighed by the savings on the wage bill.

Isoprofit curve

$$
\begin{aligned}
\pi=L(y-w) & =\bar{\pi} \\
d L(y-w)-L d w & =0 \\
\frac{d L}{d w} & =\frac{L}{y-w} \quad \frac{d L}{d w}>0 \text { for } y>w
\end{aligned}
$$

Profit maximisation at the tangency point between an isoprofit curve and the labour supply schedule

- A minimum wage - if it is not too high - raises both the wage and employment in a monopsonistic market
- Non-monotonic relationship between minimum wage and employment in a monopsonistic market


Figure 5.4
The monopsony model.

Sources of monopsony power

- Workers must have limited mobility
- transportation cost
- qualifications that cannot be used elsewhere
- Entry costs must prevent entry of competitors

Simple game-theoretic model for why the existence of entry costs can uphold a monopsony
$N$ firms can enter $c$ is the entry cost
Each worker produces $y$
Stage 1: entry decision
Stage 2: wage decision

- Solve the model backwards
- If only one firm it sets the monopsony wage If there are $\boldsymbol{n}>\mathbf{1}$ competitors, firm $\boldsymbol{i}$ sets its wage $\boldsymbol{w}_{i}$ so as to maximise its profit $\pi_{i}=L_{i}\left(y-w_{i}\right)$ taking the wages of other firms as given

Employment $L_{i}$ in firm $i$ depends on all wages $\left(w_{i}, \ldots \ldots w_{n}\right)$ in the following way:
$L_{i}=L^{s}\left(w_{i}\right)$ if $w_{i}>w_{j}, \quad \forall j \neq i$
$L_{i}=(1 / J) L^{s}\left(w_{i}\right)$ if $i$ sets the highest wage together with $J-1$ other firms, $1<\boldsymbol{J}<\boldsymbol{n}$
$L_{i}=0$ if there exists one firm $\boldsymbol{j} \neq \boldsymbol{i}$ which sets $\boldsymbol{w}_{\boldsymbol{i}}<\boldsymbol{w}_{\boldsymbol{j}}$

- All wages equal to $\boldsymbol{y}$ is a Nash equilibrium
- Then each firm has zero profits and cannot improve its profits
- with a lower wage all labour disappears
- with a higher wage it makes a loss
- No single firm can set $w_{i}<y$.
- it would then make a profit
- hence it would pay for a competitor to raise the wage above $w_{i}$ and capture the whole labour supply
- This is so-called Bertrand competition, which forces the wage up to the competitive level


## Stage 1 decision

- Each firm knows that
(i) it will make zero profits with competitors present in the market
(ii) it will make monopsony profits if it alone enters
- Once a firm has entered it does not pay for any other firm to enter
- profits will be zero
- but an entry cost $c$ has to be paid
- the first firm (if possibilities to enter come sequentially) chooses to enter if $\pi\left(w^{M}\right)>c$.
- Extreme assumptions here regarding Bertrand competition but good illustration of how entry costs may give rise to monopsony and wage differences to other sectors unrelated to productivity.


## Collective bargaining

- Common assumption for unions: identical members
- $N$ identical members in the union's "labour pool"
- Indirect utility function for the individual, increasing in income
- Every member supplies one unit of labour if the real wage $w$ exceeds the reservation wage $\bar{w}$ (= income of an unemployed person)
- $L=$ Labour demand
- Same probability of getting a job for every union member = $L / N$ if $L<N$ and unity if $L \geq N$
- Probability of unemployment $\left(1-\frac{L}{N}\right)$ if $L<N$ and zero if $L \geq N$. N


## Union objective

Maximise the expected utility of members
$\nu_{s}=l \nu(w)+(1-l) \nu(\bar{w}) \quad l=\operatorname{Min}(1, L / N)$
If $N$ is exogenous, this is equivalent to maximising the unweighted sum of members' utilities:
$L \nu(w)+(N-L) \nu(\bar{w})$
If workers are risk-neutral so that $\nu(w)=w$ and $\nu(\bar{w})=\bar{w}$, unions maximise the rent from unionisation:

$$
l w+(1-l)(\bar{w})=l(w-\bar{w})+\bar{w}
$$

If $\bar{w}=0$, this is equivalent to maximising the wage bill: $l w$

Table 3.1
Coverage of collective agreements and unionisation ${ }^{\text {² }}$

| Country | Total cconomy (2001) |  | Market sector (mid 1990s) |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Coverage | Unionisation | Coverage | Unionisation |
| Old EU member states |  |  |  |  |
| Austria | 98 | 40 | 97 | 34 |
| Belgium | 100 | 69 | 82 | 44 |
| Denmark | 85 | 88 | 52 | 68 |
| Finland | 90 | 79 | 67 | 65 |
| France | 90 | 9 | 75 | $<4$ |
| Germany | 67 | 30 | 80 | 25 |
| Greece |  | 32 |  |  |
| Ireland |  |  |  | 43 |
| Italy |  | 35 |  | 36 |
| Luxemburg | 60 | 50 |  |  |
| Netherlands | 78 | 27 | 79 | 19 |
| Portugal | 62 | 30 | 80 | $<20$ |
| Spain | 81 | 15 | 67 | $<15$ |
| Sweden | 94 | 79 | 72 | 77 |
| UK ${ }^{\text {b }}$ | 36 | 29 | 35 | 19 |
| New EU member states |  |  |  |  |
| Cyprus | 65-70 | 70 |  |  |
| Czech Republic | 25-30 | 30 |  |  |
| Estonia | 29 | 15 |  |  |
| Hungary | 34 | 20 |  |  |
| Latvia | $<20$ | 30 |  |  |
| Lithuania | 10-15 | 15 |  |  |
| Malta | 60-70 | 65 |  |  |
| Poland | 40 | 15 |  |  |
| Slovakia | 48 | 40 |  |  |
| Slovenia | 100 | 41 |  |  |
| Other countries |  |  |  |  |
| Australia | $22(23)^{\text {c }}$ | 23 |  |  |
| Canada | 32 | $30^{8)}$ |  |  |
| Japan | 21 | $22^{\text {b }}$ ) | 21 | 24 |
| New Zealand | $45^{\text {d) }}$ | 22 |  |  |
| Norway | 70-77 ${ }^{\text {e }}$ | $55^{\text {b) }}$ | 62 | 44 |
| Switzerland | $53^{7}$ | $23^{\text {b) }}$ | 50 | 22 |
| US | 15 | $14^{\text {b) }}$ | 13 | 10 |
| Notes: ${ }^{2}$ Coverage refers to the percentage of employees covered by collective agreements and unionisation to the percentage of employees with union membership; ${ }^{\text {b) }}$ Figures do not include Northern Ireland; ${ }^{\text {c }}$ The parenthesis refers to the coverage of wage awards (see Section 1.1) and to 2000; d) 1997 ; ${ }^{\text {e }} 2000-01$; ${ }^{n} 1994 ;{ }^{8} 2000$; ${ }^{\text {n }} 1996-98$. |  |  |  |  |

Fig. 3.1

## UNIONISATION TRENDS IN WESTERN EUROPE AND THE UNITED STATES



Source: Ebbinghaus and Visser (2000).
EEAG Report 2004


EEAG Report
Sources: Industrial Relations in the EU Member States and Candidate Countries (2002), Collective Bargaining Cond
Etension Procedures (2002), individual Eiroline country reports. For New Zealand: Bray and Walsh (1998).
Chapter 3

- Assumption of identical union members is convenient and has microeconomic underpinnings
- But in reality members are heterogeneous
- Restrictive assumptions necessary for collective decisionmaking
- majority decisions
- sincere voting: no attempts to influence voting by announcing intentions beforehand
- voting on a single question
- single-peaked preferences
- then the median-voter theorem can be applied
- Restrictive assumption for union decision-making
- voting only about the wage
- Conflicts between union leadership and membership
- leadership may want to maximise union size
- union size may increase with employment
- boss-dominated unions show more wage restraint


## Empirical studies of union goals

Stone-Geary utility function

$$
\nu_{s}=\left(w-w_{0}\right)^{\theta}\left(L-L_{0}\right)^{1-\theta} \quad \theta \in[0,1]
$$

## Special cases

$\theta=1 / 2, w_{0}=0, L_{0}=0 \Rightarrow$ wage bill maximisation
$\theta=1 / 2, w_{0}=\bar{w}, \mathbf{L}_{0}=\mathbf{0} \Rightarrow$ rent maximisation

## Pencavel (1984) used Stone-Geary utility function

## Decision problem

$$
\operatorname{Max}_{w} \quad \nu_{s}=\left(w-w_{0}\right)^{\theta}\left(L-L_{0}\right)^{1-\theta}
$$

s.t. $\quad L=\alpha_{0}+\alpha_{1}\left(w / r_{1}\right)+\alpha_{2}\left(r_{2} / r_{1}\right)+\alpha_{3} x+\alpha_{4} D$
$r_{1}=$ output price
$r_{2}=$ production cost
$x=$ output
$D=$ Dummy variable

## FOC:

$\frac{\theta}{\theta-1}=\frac{\alpha_{1}\left(w-w_{0}\right)}{r_{1}\left(L-L_{0}\right)}$

Estimation of labour demand function and FOC gives estimates of $\theta, w_{0}, L_{0}, \alpha_{0}, \alpha_{1}, \alpha_{2}, \alpha_{3}$ and $\alpha_{4}$.

- Not rent or wage bill maximisation
- Different $\theta$, but tendency for $\theta$ to be low
- $w_{0}$ and $L_{0}$ increase with the size of the union


## Carruth and Oswald (1985)

- Rejection of risk neutrality (and wage bill and rent maximisation)
- CRRA $=-w \nu^{\prime \prime}(w) / \nu^{\prime}(w) \approx 0.8$
- Risk neutrality implies $-w \nu^{\prime \prime}(w) / \nu^{\prime}(w)=-\mathrm{w} \cdot 0 / 1=0$
- $\frac{w^{1-\delta}}{1-\delta} ; \delta$ is CRRA

Standard right-to-manage model

- Bargaining about wages
- Employer determines employment unilaterally


## Union objective

$\nu_{s}=l \nu(w)+(1-l) \nu(\bar{w}) \quad l=\operatorname{Min}(1, L / N)$

Firm profit
$\pi=R(L)-w L$
$R^{\prime}>0, R^{\prime \prime}<0$

Labour demand from profit maximisation

$$
\begin{gathered}
\frac{\partial \pi}{\partial L}=R^{\prime}(L)-w=0 \\
w=R^{\prime}(L) \\
L^{d}(w)=R^{(-1)}(w)
\end{gathered}
$$

## In case of disagreement

- Workers get the utility of unemployed persons
- Firms get zero profit
$\gamma$ denotes relative bargaining strength of the union: $0<\gamma<1$

Apply Nash bargaining solution

$$
\begin{aligned}
& \underset{w}{\operatorname{Max}}\left(\nu_{s}-\nu_{0}\right)^{\gamma}\left(\pi-\pi_{0}\right)^{1-\gamma} \\
& \pi_{0}=\text { Profit in case of disagreement } \\
& \nu_{0}=\text { union utility in case of disagreement } \\
& \pi_{0}=0 \\
& \nu_{0}=\ell \nu(\bar{w})+(1-\ell) \nu(\bar{w})=\nu(\bar{w}) \\
& \nu_{s}-\nu_{0}=\ell \nu(w)+(1-\ell) \nu(\bar{w})-\nu(\bar{w})=\ell(\nu(w)-\nu(\bar{w}))= \\
& =\frac{L^{d}}{N}[\nu(w)-\nu(\bar{w})]
\end{aligned}
$$

$\operatorname{Max}_{w}\left[L^{D}(w)\right]^{\gamma}[\nu(w)-\nu(\bar{w})]^{\gamma}[\pi(w)]^{1-\gamma}$ with $\pi(w)=R\left[L^{D}(w)\right]-w L^{d}(w)$
s.t. $\quad L^{d}(w) \leq N$ and $w \geq \bar{w}$

Solve by taking logs and then differentiate w.r.t. $w$

## FOC:

$\frac{\gamma}{L^{d}(w)} \frac{d L^{d}(w)}{d w}+\frac{\gamma \nu^{\prime}(w)}{\nu(w)-\nu(\bar{w})}+\frac{(1-\gamma)}{\pi(w)} \frac{d \pi(w)}{d w}=0$

Note: Mistake in formula on page 394:
Second term should be

$$
\begin{aligned}
& \frac{\gamma \nu^{\prime}(w)}{\nu(w)-\nu(\bar{w})} \\
& \text { not } \\
& \frac{\gamma w \nu^{\prime}(w)}{\nu(w)-\nu(\bar{w})}
\end{aligned}
$$

Let $\eta_{w}^{L}=-(w / L)(d L / d w)$

$$
\eta_{w}^{\pi}=-(w / \pi)(d \pi / d w)
$$

Absolute values of wage elasticities of labour demand and profits

Posit $\eta_{w}^{L}=\eta_{w}^{L}\left(w, z_{L}\right) \quad \partial \eta_{\mathrm{w}}^{\mathrm{L}} / \partial_{L}^{z}>0$

$$
\eta_{w}^{\pi}=\eta_{w}^{\pi}\left(w, z_{\pi}\right) \quad \partial \eta_{w}^{\pi} / \partial_{\pi}^{z}>0
$$

$$
\begin{equation*}
\phi\left(w, \bar{w}, z_{L}, z_{\pi}, \gamma\right)=-\gamma \eta_{w}^{L}-(1-\gamma) \eta_{w}^{\pi}+\frac{\gamma w \nu^{\prime}(w)}{\nu(w)-\nu(\bar{w})}=0 \tag{3}
\end{equation*}
$$

(1)
(1) Employment loss from wage increase
(2) Profit loss from wage increase
(3) Income gain for employed workers from wage increase

Monopoly union assumption

$$
\gamma=1 \Rightarrow \eta_{w}^{L}+\frac{w \nu^{\prime}(w)}{\nu(w)-\nu(\bar{w})}=0
$$

- Still interior solution
- Trade union balances income gain for employed workers against employment loss from wage increase

SOC for a maximum is $\phi_{w}<0$

$$
\begin{gathered}
x=\left(\bar{w}, z_{L}, z_{\pi}, \gamma\right) \\
\phi_{w} d w+\phi_{x} d x=0 \\
\frac{d w}{d x}=-\frac{\phi_{x}}{\phi_{w}} \\
\phi_{w}<0 \Rightarrow \operatorname{sgn} \frac{d w}{d x}=\operatorname{sgn} \phi_{x} \\
\phi_{\gamma}=-\eta_{w}^{L}+\eta_{w}^{\pi}+\frac{w \nu^{\prime}(w)}{\nu(w)-\nu(\bar{w})}
\end{gathered}
$$

From FOC we can derive:
$-\eta_{w}^{L}+\frac{w \nu^{\prime}(w)}{\nu(w)-\nu(\bar{w})}=\frac{1-\gamma}{\gamma} \eta_{w}^{\pi}$

Substitution into expression for $\phi_{\gamma}$ gives

$$
\begin{aligned}
& \phi_{\gamma}=\eta_{w}^{\pi}+\frac{1-\gamma}{\gamma} \eta_{w}^{\pi}=\frac{\eta_{w}^{\pi}}{\gamma}>0 \\
& \because \frac{d w}{d \gamma}>0
\end{aligned}
$$

- Larger union bargaining power raises the wage

$$
\phi_{\bar{w}}=\frac{\gamma w \nu^{\prime}(w)}{[\nu(w)-\nu(\bar{w})]^{2}} \cdot \frac{\partial \nu}{\partial \bar{w}}>0
$$

- An income increase for a jobless person raises the wage

$$
\phi_{\eta_{w}^{L}}=-\gamma<0
$$

- An increase in the labour demand elasticity lowers the wage

$$
\phi_{\eta_{w}^{\pi}}=-(1-\gamma)<0
$$

- An increase in the profit elasticity lowers the wage


## Rewrite FOC:

$$
\frac{\nu(w)-\nu(\bar{w})}{w \nu^{\prime}(w)}=\frac{\gamma}{\gamma \eta_{w}^{L}+(1-\gamma) \eta_{w}^{\pi}} \equiv \mu_{s}
$$

## No bargaining power for union: $\gamma=0$

Hence: $\nu(w)=\nu(\bar{w})$

$$
w=\bar{w}
$$

- Employed workers only get a wage equal to the income of the unemployed

No bargaining power for the employer: $\gamma=1$
$\frac{\nu(w)-\nu(\bar{w})}{w \nu^{\prime}(w)}=\frac{1}{\eta_{w}^{L}}$

- The mark-up factor only depends on the elasticity of labour demand.


## Union indifference curves in $w, L$-space

$$
\begin{aligned}
& \bar{U}=L[\nu(w)-\nu(\bar{w})] \\
& 0=L \nu^{\prime}(w) d w+d L[\nu(w)-\nu(\bar{w})]
\end{aligned}
$$

$$
\frac{d w}{d L}=\left.\right|_{\bar{U}=\text { const }}=-\frac{[\nu(w)-\nu(\bar{w})]}{L \nu^{\prime}(w)} \leq 0
$$

$$
\frac{d^{2} w}{d L^{2}}=\left.\right|_{\bar{U}=\mathrm{const}}=\frac{[\nu(w)-\nu(\bar{w})]}{L^{2}\left[\nu^{\prime}(w)\right]^{2}}\left\{2 \nu^{\prime}(w)-\nu^{\prime \prime}(w) \frac{[\nu(w)-\nu(\bar{w})]}{\nu^{\prime}(w)}\right\} \geq 0
$$

Union indifference curves are negatively sloped and convex.


Figure 7.5
The right-to-manage model.

## Isoprofit curves

$$
\bar{\pi}=R(L)-w L
$$

$$
R^{\prime}(L) d L-w d L-L d w=0
$$

$$
\left.\frac{d w}{d L}\right|_{\pi=\bar{\pi}}=\frac{R^{\prime}(L)-w}{L}
$$

$$
d\left[\left.\frac{d w}{d L}\right|_{\pi=\bar{\pi}}\right]=\frac{L\left[R^{\prime \prime}(L) d L-d w\right]-d L\left[R^{\prime}(L)-w\right]}{L^{2}}=
$$

$$
\left.\frac{d^{2} w}{d L^{2}}\right|_{\pi=\bar{\pi}}=\frac{L R^{\prime \prime}(L)}{L^{2}}-\frac{\frac{d w}{d L}}{L^{2}}-\frac{\left[R^{\prime}(L)-w\right]}{L^{2}}
$$

$$
\begin{aligned}
& \text { Substitute } \frac{R^{\prime}(L)-w}{L} \text { for } \frac{d w}{d L} \text { : } \\
& \left.\frac{d^{2} w}{d L^{2}}\right|_{\pi=\bar{\pi}}=\frac{L R^{\prime \prime}(L)}{L^{2}}-\frac{R^{\prime}(L)-w}{L^{2}}-\frac{R^{\prime}(L)-w}{L_{2}} \\
& =\frac{L R^{\prime \prime}(L)-2\left[R^{\prime}(L)-w\right]}{L^{2}}
\end{aligned}
$$

- Choosing $L$ to maximise profit implies $\mathbf{R}^{\prime}(L)=w$. Hence isoprofit curve is horizontal where it intersects the labour demand schedule.
- At intersection with labour demand schedule, $R^{\prime}(L)=w$.

Hence $\left.\frac{d^{2} w}{d L^{2}}\right|_{\pi=\bar{\pi}}=\frac{R^{\prime \prime}(L)}{L}<0$.
Isoprofit curves are concave there, which imply maxima.

## General FOC:

$-\gamma \eta_{w}^{L}-(1-\lambda) \eta_{w}^{\pi}+\frac{\gamma w \nu^{\prime}(w)}{\nu(w)-\nu(\bar{w})}=0$

- If $\eta_{w}^{L}, \eta_{w}^{\pi}, \gamma$ and $\bar{w}$ are constants, then the real wage $w$ is constant as well. It will not be affected by an iso-elastic shift of the labour demand schedule (for example because of a productivity shock).
- Constant $\eta_{w}^{L}$ and $\eta_{w}^{\pi}$ will occur if the revenue function is CobbDouglas.


## Simplified model

$$
\pi=R(L)-w L=\frac{A L^{\alpha}}{\alpha}-w L \quad \alpha \in(0,1)
$$

## Profit maximisation gives:

$$
\frac{\partial \pi}{\partial L}=A L^{\alpha-1}-w=0
$$

$$
L=\left(\frac{W}{A}\right)^{\frac{1}{\alpha-1}}
$$

Then:
$\pi=\frac{A}{\alpha} \cdot\left(\frac{w}{A}\right)^{\frac{\alpha}{\alpha-1}}-w \cdot\left(\frac{w}{A}\right)^{\frac{1}{\alpha-1}}$
$\pi=W^{\frac{\alpha}{\alpha-1}} \cdot \frac{1-\alpha}{\alpha} A^{\frac{1}{\alpha-1}}$

Hence:
$\eta_{w}^{L}=-\frac{\partial L}{\partial w} \cdot \frac{L}{w}=\frac{1}{1-\alpha}$
$\eta_{w}^{\pi}=-\frac{\partial L}{\partial w} \cdot \frac{w}{\pi}=\frac{\alpha}{1-\alpha}$

Also assume that $\nu(w)=w$ and $\nu(\bar{w})=\bar{w}$
Then $\nu^{\prime}(w)=1$

FOC (A) then becomes:
$-\gamma \cdot \frac{1}{1-\alpha}-(1-\gamma) \frac{\alpha}{1-\alpha}+\frac{\gamma w}{w-\bar{w}}=0$
Solving for $w$ gives:
$w=\frac{\gamma+\alpha(1-\gamma)}{\alpha} \bar{w}$

The wage is set as a mark-up on the income of an unemployed, since $\gamma+\alpha(1-\gamma)>\alpha \Leftrightarrow \gamma(1-\alpha)>0$, which must hold.

Especially simple form in monopoly-union case, i.e. if $\gamma=1$
Then $w=\frac{\bar{w}}{\alpha}$
We have:

$$
\eta_{\mathrm{w}}^{\mathrm{L}}=\frac{1}{1-\alpha}
$$

Hence:

$$
\begin{aligned}
& 1-\alpha=\frac{1}{\eta_{\mathrm{w}}^{\mathrm{L}}} \\
& \alpha=1-\frac{1}{\eta_{\mathrm{w}}^{\mathrm{L}}}=\frac{\eta_{\mathrm{w}}^{L}-1}{\eta_{\mathrm{w}}^{L}}
\end{aligned}
$$

Thus:
$w=\left[1-\frac{1}{\eta_{w}^{L}}\right]^{-1} \bar{w}$
$w=\frac{\eta_{w}^{L}}{\eta_{w}^{L}-1} \bar{w}$

Analogy to monopoly price setting with price as a mark-up over marginal cost
$\eta_{w}^{L}>1$ is always the case with Cobb-Douglas production function,
as $\eta_{w}^{L}=\frac{1}{1-\alpha}$ and $0<\alpha<\mathbf{1}$.

## General equilibrium model

$$
w_{i}=\frac{\gamma+\alpha(1-\gamma)}{\alpha} \bar{w}
$$

- Assume mobility in the labour market. An unemployed in a given firm (labour pool) can either find a job in another firm (labour pool) or become unemployed.
- Symmetric economy with a large number of firms.
- Look at wage-setting in firm i.
- Probability of getting a job in another firm = I = the economy-wide employment rate = employment/labour force.
- Probability of not finding a job elsewhere = 1-I.
- A worker who finds a job elsewhere receives the wage $w$.
- If unemployed, the worker receives the unemployment benefit $b$.
$\bar{w}=$ the expected income if not employed in firm $i=$ alternative income

$$
\bar{w}=\ell w+(1-\ell) b
$$

Hence:
$w_{i}=\frac{\gamma+\alpha(1-\gamma)}{\alpha}[\ell w+(1-\ell) b]$
In a symmetric equlibrium $w_{i}=w$
Denote the mark-up factor $\frac{\gamma+\alpha(1-\gamma)}{}=m$
$\alpha$
Then:

$$
\begin{align*}
& w=m[\ell w+(1-\ell)] b \\
& w=\frac{m(1-\ell)}{1-m \ell} b \tag{B}
\end{align*}
$$

- The wage is still a mark-up over the unemployment benefit as

$$
m(1-\ell)>1-m \ell \Leftrightarrow m>1
$$

- The overall wage in the economy, $w$, is positively related to employment as:

$$
\frac{\partial w}{\partial \ell}=\frac{m(m-1)}{(1-m \ell)^{2}}>0
$$

$w=f(I)$ is called a wage-setting schedule
It shifts upwards if:
(1) $\gamma \uparrow$
(2) $\boldsymbol{b} \uparrow$

- Equilibrium employment is given by intersection between the wage-setting schedule and the labour-demand schedule.
- Shift of labour-demand schedule affects the equilibrium employment rate.


Key question: How is the unemployment benefit determined?

1. Constant in real terms
2. Constant replacement rate $r$, so that $b=r w$

## Constant replacement rate:

$$
\begin{aligned}
& w=\frac{m(1-\ell)}{1-m \ell} b \\
& w=\frac{m(1-\ell)}{1-m \ell} r w
\end{aligned}
$$

$$
1=\frac{m(1-\ell)}{1-m \ell} r
$$

$$
\ell=\frac{1-r m}{m(1-r)}
$$

$$
\frac{\partial \ell}{\partial r}=\frac{m(1-m)}{(m-r)^{2}}<0
$$

- Vertical wage-setting schedule determined by labour-market institutions only (here $r$ and $\gamma$ )
- An increase in the replacement rate reduces the employment rate
- Shifts in labour demand have no effect on the equilibrium employment rate.


